UNIT I - ALGORITHM ANALYSIS

PART-A (2 MARKS)

1. Define algorithm.
2. What is big ‘Oh’ notation?
3. Define Loop.
4. What are the two different types of recurrence
5. State the best case and worst case analysis for linear search.
6. Solve the recurrence equation.
   \[ T(n) = 2T(n-1) + n2^n + n^2. \]
7. Give the recurrence equation for the worst case behavior of merge sort.
8. What is the average case complexity of linear search algorithm?

PART-B

1. (a). Define the asymptotic notations used for best case average case and worst case analysis of algorithm. (8)
   (b) Write an algorithm for finding maximum element of an array; perform best and average case complexity with appropriate order notations. (8)
2. Write an algorithm to find mean and variance of an array perform best, worst and average case complexity, defining the notations used for each type of analysis. (16)
3. Derive the recurrence relation for Fibonacci series, perform complexity analysis for the same. (16)
4. Explain the various asymptotic notations with the properties. (16)
5. Explain linear search with example (16)
UNIT II - DIVIDE AND CONQUER

PART-A (2 MARKS)

1. Define Substitution method.
2. Analysis the various cases of complexity for Binary search.
3. Define Control Abstraction.
5. What is the computing time of DAndC.
6. Write the complexity of divide and Conquer algorithms.
7. Sort the numbers using merge sort.
8. List out the disadvantage of merge sort.
9. What are the four feasible solutions for 
   \( n=3, m=20, (p_1, p_2, p_3) = (25, 24, 15), (w_1, w_2, w_3) = 18, 15, 10 \).
10. Give the time efficiency and drawback of merge sort algorithm.
11. Write a pseudo code for a divide and conquer algorithm for finding the position of 
    the largest element in an array of N numbers.
12. What is recursive call?
13. What are objectives of sorting Algorithms?
14. List out any two drawbacks of binary search algorithm.
15. Write the procedure for selection sort.

PART-B

1. Explain Knapsack Problem 
   (16).
2. Explain the algorithm for maximum and minimum numbers in an array. 
   (16)
3. (a) Give a detailed note on Divide and Conquer techniques. (6)
    (b). Sort the following set of elements using merge sort 
    12, 24, 8, 71, 4, 23, 6, 89, 56
   (16)
5. (a) write a pseudo code for a divide and conquer algorithm for 
    merging two sorted arrays into a single sorted one. Explain with an example. 
    (12)
    (b) Setup an solve a recurrence relation for the number of key 
    comparisons made by the above pseudo code. 
    (4)
6. (a) Write an algorithm to sort a set of N numbers using insertion sort. (8)
    (b) Trace the algorithm for the following set of numbers. 
    20, 35, 18, 8, 14, 41, 3, 39.
7. Explain in detail merge sort. Illustrate the algorithm with a numeric example. Provide complete analysis of the same 
   (16)
UNIT III - DYNAMIC PROGRAMMING

PART-A (2 MARKS)

1. Write any four examples for Brute Force Approach.
2. Define Dynamic programming.
3. Define multistage graph problem.
4. What is the difference between forward & backward approach?
5. Define all-pair shortest path problem.
6. Draw a graph for the following matrix
   \[
   \begin{matrix}
   \infty & 0 & 1 \\
   -2 & 0 & 1 \\
   \infty & \infty & 0 \\
   \end{matrix}
   \]
8. What is 0/1 Knapsack.
9. What is the procedure to solve traveling Salesman problem.
10. Differentiate non preemptive & preemptive scheduling.
11. List out the advantages of Dynamic programming.

PART-B

1. Solve the all-pairs shortest path problem for the digraph with the weight matrix given below. (16)

   \[
   \begin{array}{cccc}
   A & B & C & D \\
   A & 0 & \infty & \infty & 3 \\
   B & 2 & 0 & \infty & \infty \\
   C & \infty & 7 & 0 & 1 \\
   D & 6 & \infty & \infty & 0 \\
   \end{array}
   \]

2. Solve the following instance of the single source shortest path problem with vertex ‘a’ as the source. 4

write the algorithm for the above problem.
Design and Analysis of algorithms

4. How will you construct an optimal search tree with example. (16)
5. Explain the Multistage graph with example. (16)
6. Explain the 0/1 knapsack with an algorithm. (16)
7. Describe the Traveling salesman problem & discuss how to solve it using Dynamic Programming. (16)

UNIT IV - BACKTRACKING

PART-A(2 MARKS)
1. What is m-colorability optimization?
2. Define sum of subsets problem.
3. What is chromatic numbers?
4. Define Backtracking.
5. What are the applications of backtracking?
6. What are the algorithm design techniques?
8. Define Hamiltonian Circuit problem in an undirected Graph.
9. What is state space tree?
10. State the principle of Backtracking.
11. State if Backtracking always produces optimal solution.

PART-B
1. What is Backtracking? Explain in detail. (16)
2. Explain Subset-sum Problem & Discuss the possible solution strategies using backtracking. (16)
3. Discuss the use of greedy method in solving knapsack problem and subset sum problem. (16)
4. Write short notes on
   (a) Graph coloring (8)
   (b) 8-Queens problem (8)
5. Apply Backtracking technique to solve the following instance of the subset sum problems. s=(1,3,4,5) & d=11 (16)
6. Explain subset-sum problem and discuss the possible solution strategies using backtracking. (16)
7. Explain 8-Queens problem with an algorithm. Explain why backtracking is defined as a default procedure of last resort for solving problems. (10+6)
8. Using Backtracking enumerate how can you solve the following problems
   (a) 8-queens problem (8)
   (b) Hamiltonian circuit problem (8)
UNIT V - TRAVERSALS, BRANCH AND BOUND

PART-A (2 MARKS)

1. Define Traversal of Trees.
2. What are the different ways of traversal of Trees?
3. Define connected components.
4. When do you say a tree as minimum spanning tree?
5. What is a minimum cost spanning tree?
6. Define depth first searching techniques.
7. Define bi connected components.
8. Compare Backtracking & Branch and Bound techniques with an example.
9. What are the applications of branch & bound?
10. Define Nondeterministic algorithms.
11. Define Deterministic algorithms.
12. What are the three function specify for Nondeterministic algorithm.

PART-B

1. Define spanning tree? Discuss the design steps in prims algorithm to construct minimum spanning tree with example. (16)
2. Explain the method of binding the minimum spanning tree for a connected graph using prims algorithm. (16)
3. Define spanning tree? Discuss the design steps in kruskal algorithm to construct minimum spanning tree with example. (16)
4. Compare and contrast the depth first search and birth first search. How do they fit in to the decrease and conquer strategies. (16)
5. Explain NP-hard and NP complete problems with example. (16)
6. Explain connected components and bi-connected components with psecdocode. (16)
7. Give a suitable example and explain the birth first search and depth first search algorithm. (16)
8. What is branch and bound? Explain detail. (16)
9. Discuss the solution for knapsack problem using branch bound techniques. (16)